

```
\documentclass{article}
\usepackage{oz} % oz or z-eves or fuzz styles
```

```
\begin{document}
This is the BirthdayBook specification, from
Spivey~\cite{spivey:z-notation2}. We extend it slightly
by adding an extra operation, $RemindOne$, that is non-deterministic.
```

```
\begin{zed}
  [NAME, ~ DATE]
\end{zed}
```

The \$BirthdayBook\$ schema defines the \emph{state space} of the birthday book system.

```
\begin{schema}{BirthdayBook}
  known: \power NAME \
  birthday: NAME \pfun DATE
\where
  known=\dom birthday
\end{schema}
```

This \$InitBirthdayBook\$ specifies the initial state of the birthday book system. It does not say explicitly that \$birthday'\$ is empty, but that is implicit, because its domain is empty.

```
\begin{schema}{InitBirthdayBook}
  BirthdayBook~'
\where
  known' = \{ \}
\end{schema}
```

Next we have several operation schemas to define the normal (non-error) behaviour of the system.

```
\begin{schema}{AddBirthday}
  \Delta BirthdayBook \
  name?: NAME \
  date?: DATE
\where
  name? \notin known
\\
  birthday' = birthday \cup \{name? \mapsto date?\}
\end{schema}
```

```
\begin{schema}{FindBirthday}
  \Xi BirthdayBook \
  name?: NAME \
  date!: DATE
\where
  name? \in known
\\
```

```

    date! = birthday(name?)
\end{schema}

\begin{schema}{Remind}
  \Xi BirthdayBook \\\
  today?: DATE \\\
  cards!: \power NAME
\where
  cards! = \{ n: known | birthday(n) = today? \}
\end{schema}

```

This \$RemindOne\$ schema does not appear in Spivey, but is included to show how non-deterministic schemas can be animated. It reminds us of just one person who has a birthday on the given day.

```

\begin{schema}{RemindOne}
  \Xi BirthdayBook \\\
  today?: DATE \\\
  card!: NAME
\where
  card! \in known \\\
  birthday ~ card! = today?
\end{schema}

```

Now we strengthen the specification by adding error handling.

```

\begin{zed}
  REPORT ::= ok | already\_known | not\_known
\end{zed}

```

First we define auxiliary schemas that capture various success and error cases.

```

\begin{schema}{Success}
  result!: REPORT
\where
  result! = ok
\end{schema}

```

```

\begin{schema}{AlreadyKnown}
  \Xi BirthdayBook \\\
  name?: NAME \\\
  result!: REPORT
\where
  name? \in known \\\
  result! = already\_known
\end{schema}

```

```

\begin{schema}{NotKnown}
  \Xi BirthdayBook \\\
  name?: NAME \\\

```

```

    result!: REPORT
\where
    name? \notin known \
    result! = not\_known
\end{schema}

```

Finally, we define robust versions of all the operations by specifying how errors are handled. For illustration purposes, we leave the \$RemindOne\$ operation non-robust.

```

\begin{zed}
    RAddBirthday == (AddBirthday \land Success) \lor AlreadyKnown \
    RFindBirthday == (FindBirthday \land Success) \lor NotKnown \
    RRemind == Remind \land Success
\end{zed}

\bibliography{spec}
\begin{thebibliography}{1}
\bibitem{spivey:z-notation2}
J.~Michael Spivey.
\newblock {\em The Z Notation: A Reference Manual}.
\newblock International Series in Computer Science. Prentice-Hall International
(UK) Ltd, second edition, 1992.
\end{thebibliography}
\end{document}

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